

Computation of photoemission spectra of the doped Mott insulator $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$ using LDA+DMFT(QMC)

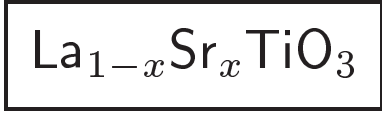
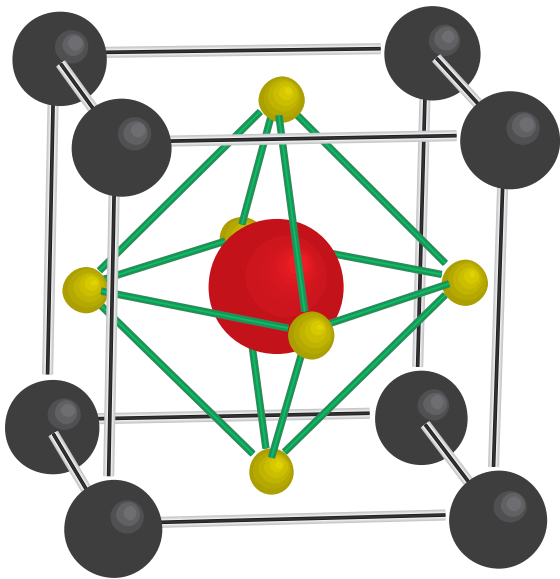
N. Blümer, I.A. Nekrasov, K. Held, A.I. Poteryaev,
V.I. Anisimov, and D. Vollhardt

Eur. Phys. J. B **18**, 55 (2000); cond-mat/0010395

Outline

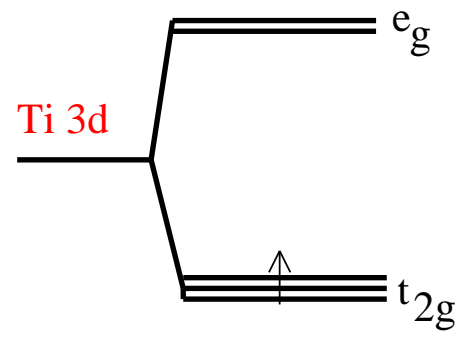
- Introduction: Structure of $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$; experimental PES
- Theory: DFT(LDA); extensions for strong correlations
dynamical mean-field theory (DMFT)
quantum Monte Carlo (QMC)
- Results: t_{2g} density of states; theoretical PES

Introduction

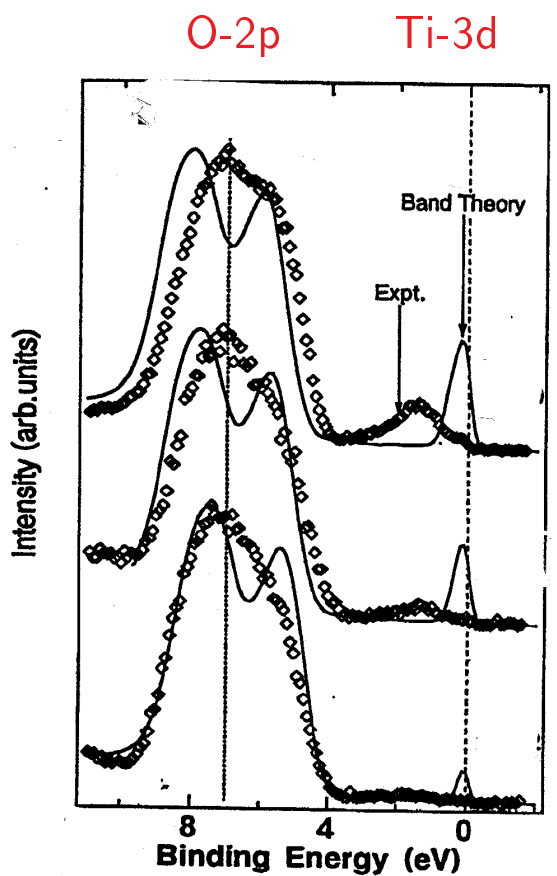


- La, Sr
- Ti
- O

Cubic Perovskite
slight orthorhombic distortion



- $x = 0$ LaTiO_3 : AF insulator for $T < T_N = 125\text{K}$
- $x > 0.05$ strongly correlated paramagnetic metal
- $x = 1$ SrTiO_3 : band insulator



x photoemission spectra (PES)

- 0.06
- 0.5
- 0.8

- LDA fails when correlations become strong
- $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$ ($x \ll 1$) is typical strongly correlated transition metal oxide

[Fujimori et al., PRB 46, 9841 (1992)]

Theory

DFT/LDA	Model Hamiltonians
+ material specific: “ab initio”	– input parameters unknown
– fails for strong correlations	+ systematic many-body approach
+ fast code packages	– computationally expensive

Density functional theory (Hohenberg-Kohn, Levy): $E_0 = E_0[\rho]$

$$E[\rho] = E_{\text{kin}}[\rho] + E_{\text{ion}}[\rho] + E_{\text{Hartree}}[\rho] + E_{\text{xc}}[\rho]$$

local density approximation (LDA): $E_{\text{xc}}[\rho] \rightarrow \int d^3r E_{\text{xc}}^{\text{jellium}}(\rho(\mathbf{r}))$

interpret Kohn-Sham Lagrange parameters as single-particle energies
use localized basis (linear muffin tin orbitals, LMTO)

→ tight-binding Hamiltonian

$$\hat{H}^{\text{LMTO}} = \sum_{ilm,jl'm',\sigma} \left(t_{ilm,jl'm'} \hat{c}_{ilm,\sigma}^\dagger \hat{c}_{jl'm',\sigma} + \varepsilon_{ilm} \hat{n}_{ilm,\sigma} \delta_{ilm,jl'm'} \right)$$

LDA+U: introduces Hubbard U for localized orbitals ($l = l_d$, treatment in static mean-field theory) [Anisimov, Zaanen, Andersen, PRB. **44**, 943 (1991)]

here: many-body approach

$$\hat{H} = \hat{H}^{\text{LMTO}} + \frac{1}{2} \sum_{m\sigma \neq m'\sigma'} U_{mm'} \hat{n}_m^\sigma \hat{n}_{m'}^{\sigma'} - \frac{1}{2} U n_d (n_d - 1)$$

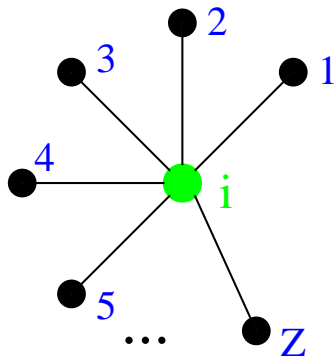
Approximation needed for treatment of \hat{H}_{corr} :

DMFT: Anisimov, Poteryaev, Korotin, Anokhin, Kotliar, J. Phys. **9**, 7359 (1997)

FLEX: Lichtenstein, Katsnelson, PRB **57**, 6884 (1998) (also Hubbard-I, DMFT)

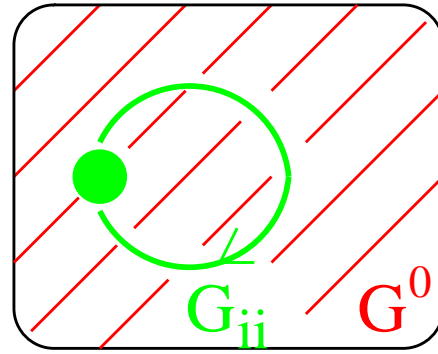
Drchal, Janiš, Kudrnovský, PRB **60**, 15664 (1999)

LDA + DMFT



lattice problem

DMFT
 $\xrightarrow{\text{exact for } Z \rightarrow \infty}$



single impurity Anderson model
 + self consistency condition

Metzner, Vollhardt, PRL **62**, 324 (1989); Georges et al., RMP **44**, 187 (1995)

For weak hybridization of t_{2g} orbital, orbital/spin-degenerate case:

$$G(z) = G^0(z - \Sigma(z)) = \int d\varepsilon \frac{\rho_0^{\text{LMTO}}(\varepsilon)}{z - \Sigma(z) - \varepsilon}$$

$$G_{\nu m \sigma} = -\langle \psi_{\nu m \sigma} \psi_{\nu m \sigma}^* \rangle_{\mathcal{A}\{\psi, \psi^*; G^{-1} + \Sigma\}}; \quad z \rightarrow \omega_\nu = \frac{(2\nu + 1)\pi}{\beta}$$

Numerical solution of LDA+DMFT(X)

- IPT Anisimov, Poteryaev, Korotin, Anokhin, Kotliar, J. Phys. **9**, 7359 (1997)
- NCA Zöfl, Pruschke, Keller, Poteryaev, Nekrasov, Anisimov, PRB **61**, 12810 (2000)
- QMC Katsnelson, Lichtenstein, PRB **61**, 8906 (2000)
- Liebsch, Lichtenstein, PRL **84**, 1591 (2000)

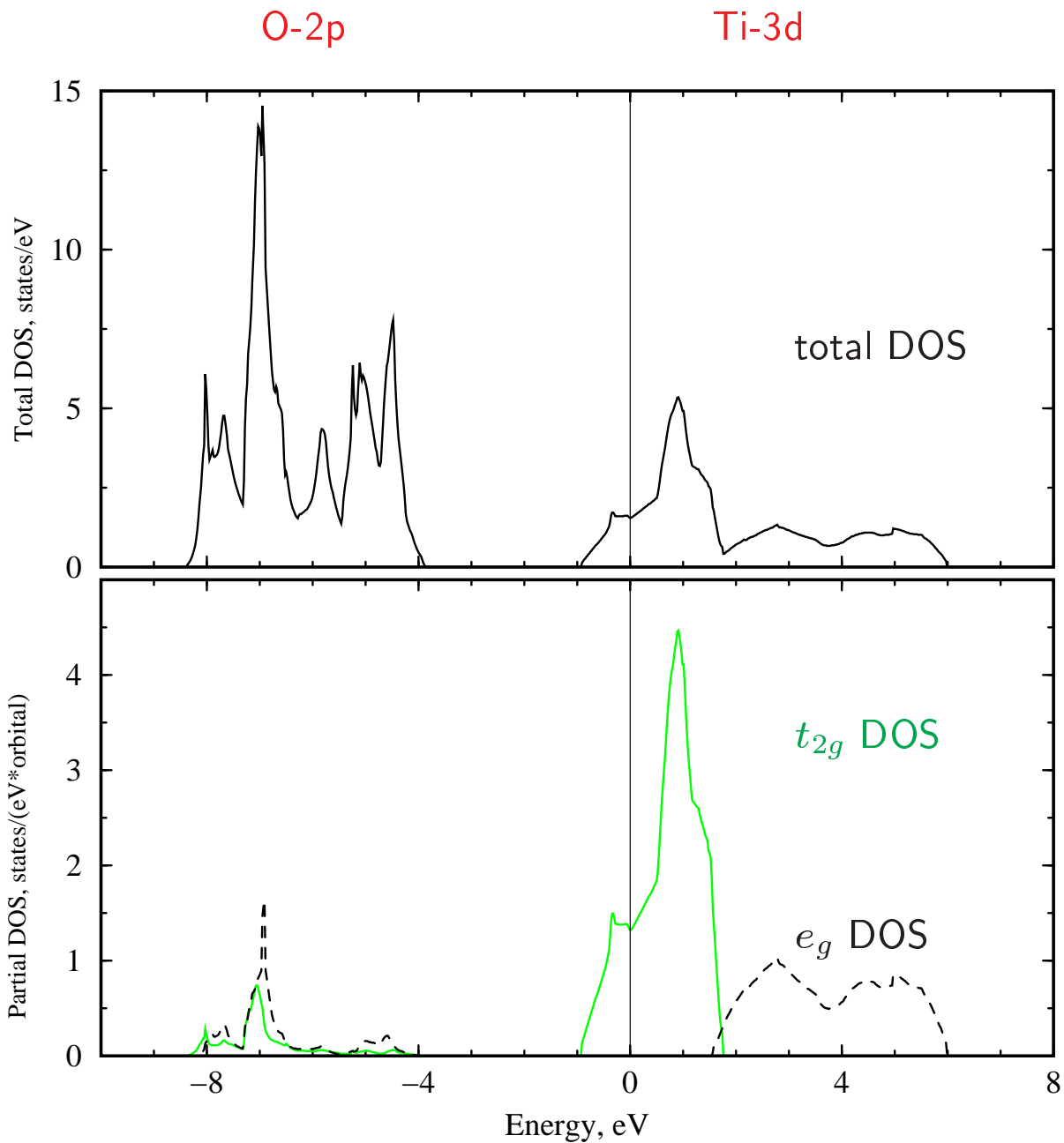
QMC solution of impurity problem (M interacting orbitals):

- discretization $\Delta\tau$ of imaginary time $\beta = \Lambda \Delta\tau$ ($\beta = 1/T$)
- discrete Hubbard-Stratonovich transformation
 $\rightarrow 2^{M(2M-1)\Lambda}$ different non-interacting systems
- MC importance sampling; computational cost $\propto M(2M - 1)\beta^3$

Hirsch and Fye, PRL **56**, 2521 (1986)

Results

LDA-LMTO(ASA) calculation for LaTiO_3

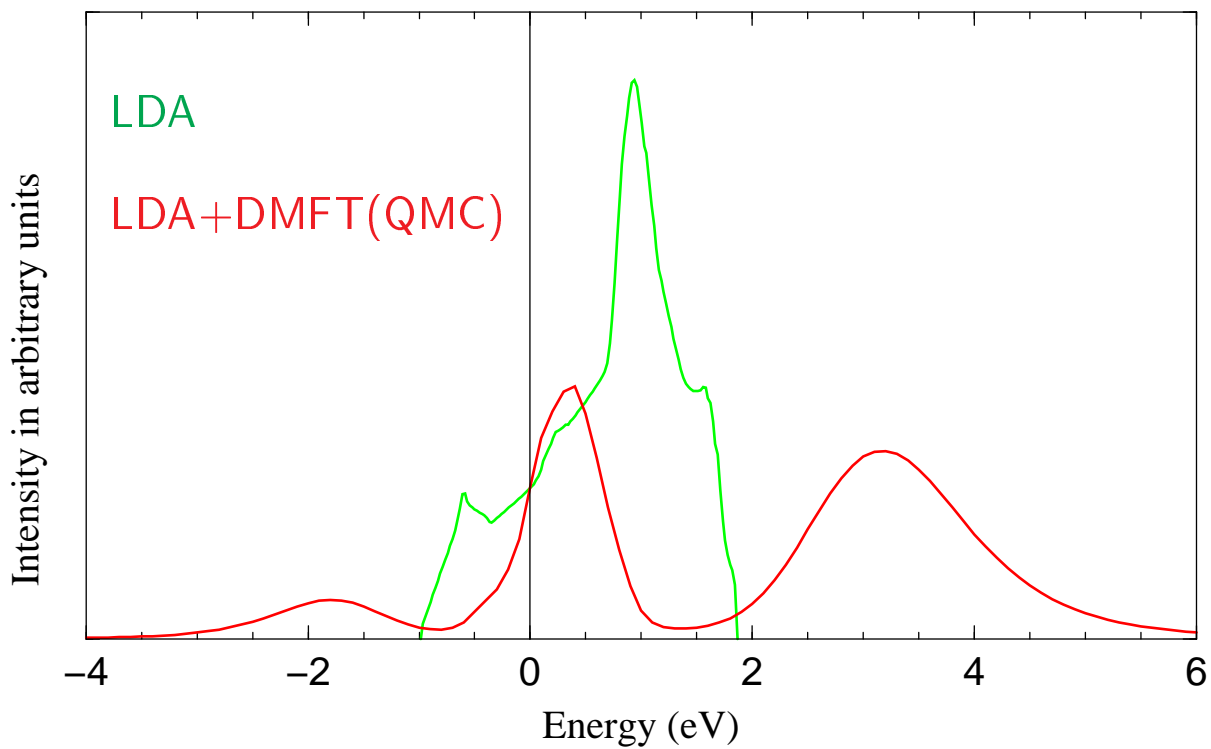


Orthorhombic structure approximated by cubic structure with same volume
→ slight overestimation of effective bandwidth

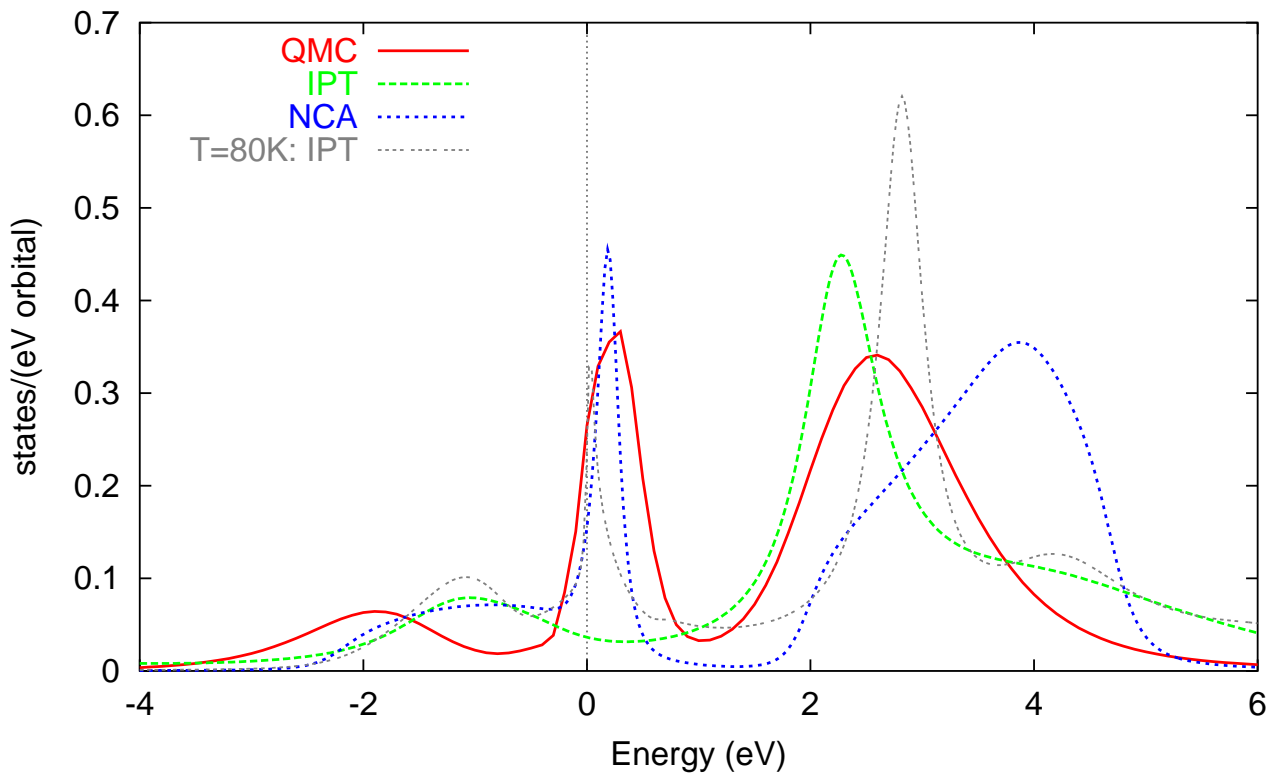
constrained LDA → $U_d \approx 3 - 5$ eV

DMFT calculation for $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$: partial t_{2g} DOS

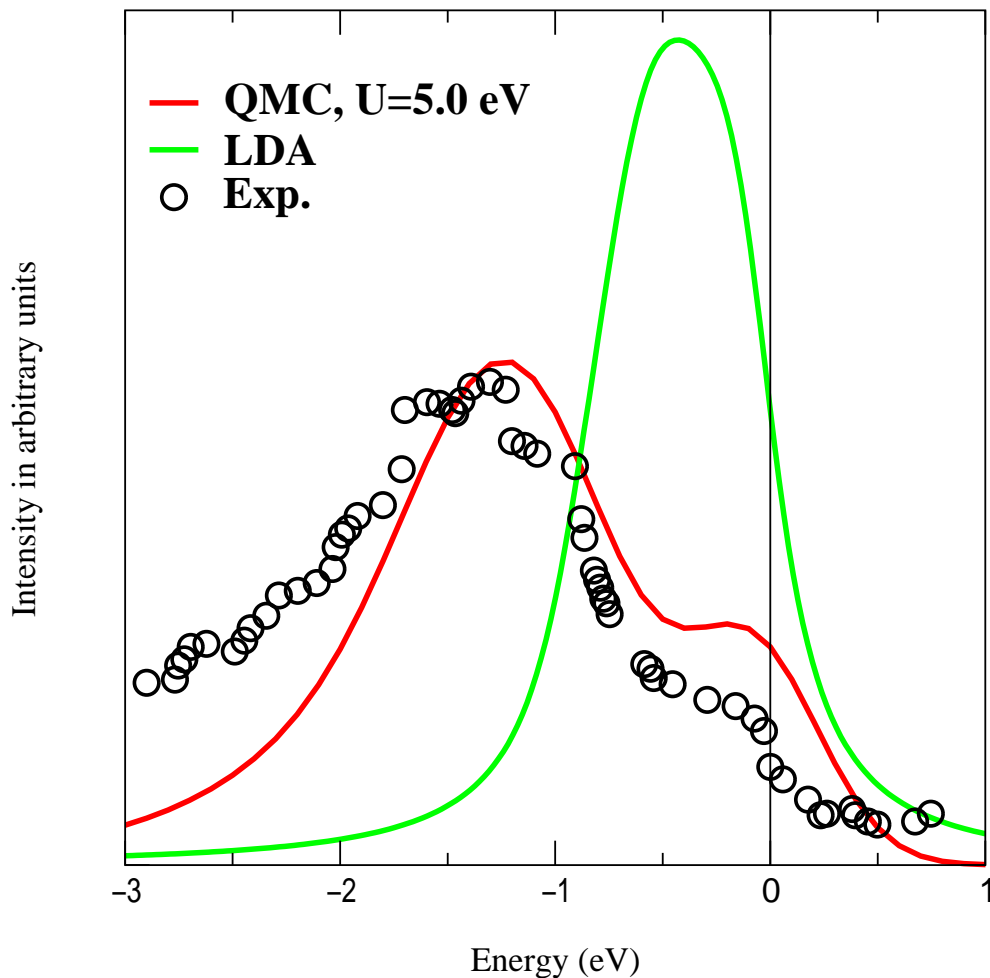
$x = 0.06$, $U = 4.0$ eV, $T = 0.1$ eV $\sim 1000\text{K}$, 3 degenerate bands



Comparison to approximate DMFT methods



Comparison with experiment: photoemission spectra (PES)



Experiment: [Fujimori et al., PRL 69, 1796 \(1992\)](#)

Theory: DOS multiplied with Fermi step function; broadening 0.3 eV

Conclusion

- LDA + DMFT(QMC) yields qualitatively correct picture
- significant improvement over LDA
- QMC solution of DMFT superior to NCA, IPT
- include more orbitals, Hund's rule couplings
- other materials: V_2O_3 (see TT 6.13; [Held et al., cond-mat/0011518](#))

Work supported by DFG through SFB 484