

Quantum Monte Carlo (QMC) Simulations within the Dynamical Mean-field Theory (DMFT)

Nils Blümer

TP6, WA Prof. van Dongen (KOMET337)

Outline

Introduction: Hubbard model, DMFT, self-energy

General Monte Carlo principles

Hirsch-Fye QMC algorithm; error bars

Mott Insulator (1 band): QMC vs. ePT and SFT/DIA

LDA+DMFT(QMC) for $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$; MEM

Summary and Preview

Introduction: Hubbard model, DMFT

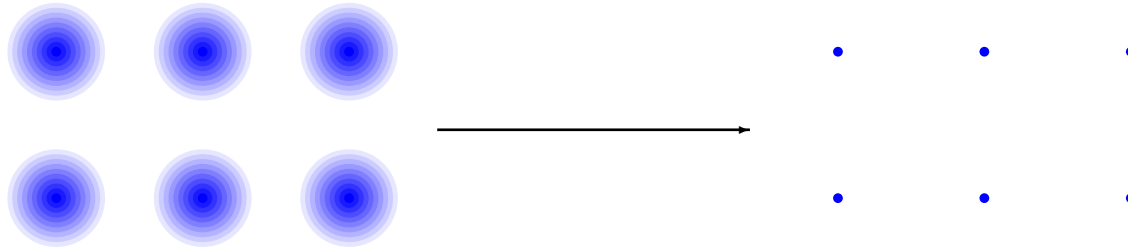
$$H = \sum_{i=1}^{N_e} \frac{\mathbf{p}_i^2}{2m} + \sum_{k=1}^L \frac{\mathbf{P}_k^2}{2M_k} + \sum_{k<l} \frac{Z_k Z_l e^2}{|\mathbf{R}_k - \mathbf{R}_l|} - \sum_{i,k} \frac{Z_k e^2}{|\mathbf{r}_i - \mathbf{R}_k|} + \sum_{i<j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|}$$

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Born-Oppenheimer approximation ↓

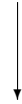
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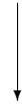
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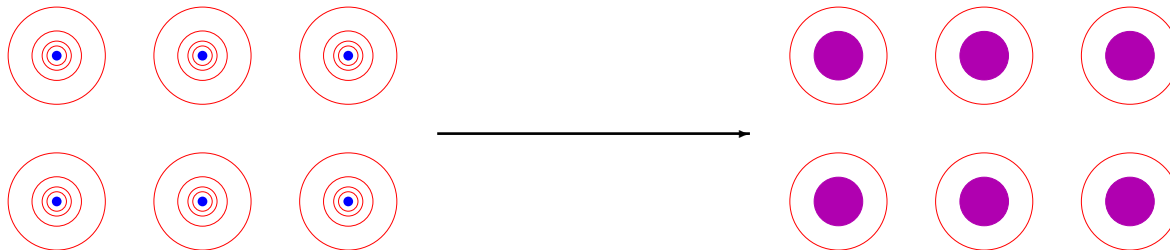


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reduction to valence electrons



$$H = \sum_{i=1}^{N_v} \frac{\mathbf{p}_i^2}{2m} + \sum_{i=1}^{N_v} V^{\text{ion}}(\mathbf{r}_i) + \sum_{i=1}^{N_v-1} \sum_{j=i+1}^{N_v} V^{ee}(\mathbf{r}_i, \mathbf{r}_j)$$



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occupation number formalism, Wannier orbitals

$$\hat{H} = \sum_{i\nu j\sigma} t_{ij}^\nu \hat{c}_{i\nu\sigma}^\dagger \hat{c}_{j\nu\sigma} + \frac{1}{2} \sum_{\nu\nu'\mu\mu'} \sum_{ijmn} \sum_{\sigma\sigma'} v_{ijmn}^{\nu\nu'\mu\mu'} \hat{c}_{i\nu\sigma}^\dagger \hat{c}_{j\nu'\sigma'}^\dagger \hat{c}_{n\mu'\sigma'} \hat{c}_{m\mu\sigma}$$

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reduction to valence electrons

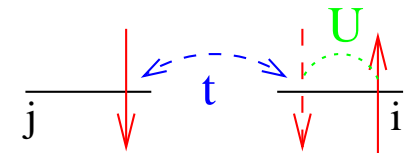
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Hubbard model

$$\hat{H} = \sum_{(i,j),\sigma} t_{ij} (\hat{c}_{i\sigma}^\dagger \hat{c}_{j\sigma} + \text{h.c.}) + U \sum_i \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}$$

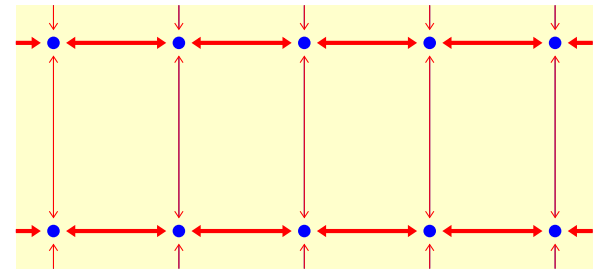


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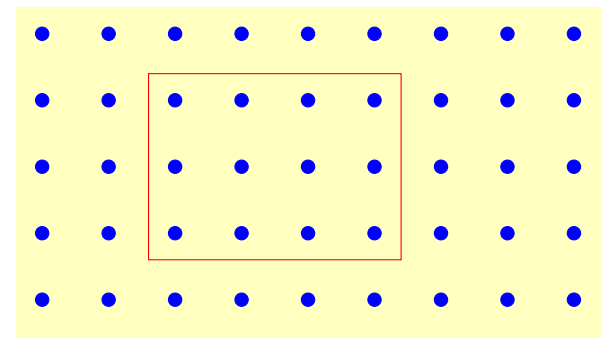
Perturbation theory, e.g.

- $U \rightarrow 0$: Hartree-Fock (**uncorrelated**)
- $t/U \rightarrow 0$: half filling ($n = 1$) \rightsquigarrow Heisenberg model
- $T \rightarrow \infty, n \rightarrow 0$
- ($V_{\text{ion}} \rightarrow 0 \rightsquigarrow$ jellium model \rightsquigarrow LDA)

$d = 1$: Bethe ansatz, DMRG

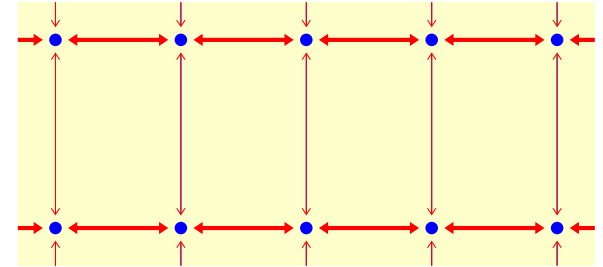


finite clusters: ED, QMC



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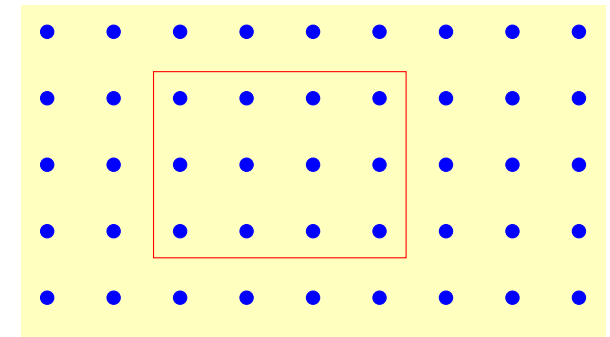
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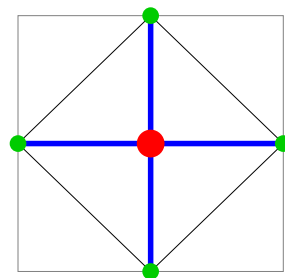
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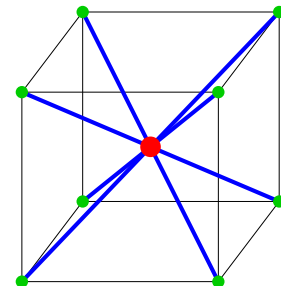


Dynamical mean-field theory (DMFT): local self-energy $\Sigma(\mathbf{k}, \omega) \equiv \Sigma(\omega)$

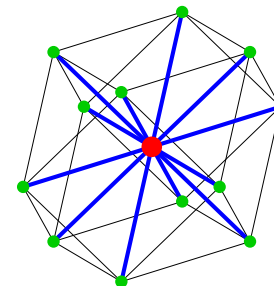
- + non-perturbative \rightsquigarrow valid at MIT
- + dynamical on-site correlations preserved
- + exact for $Z \rightarrow \infty$
- + in thermodynamic limit



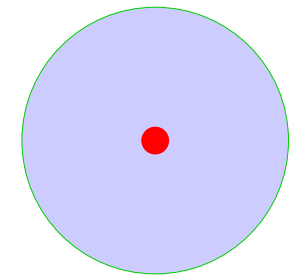
$d=2$: $Z = 4$



bcc: $Z = 8$



fcc: $Z = 12$

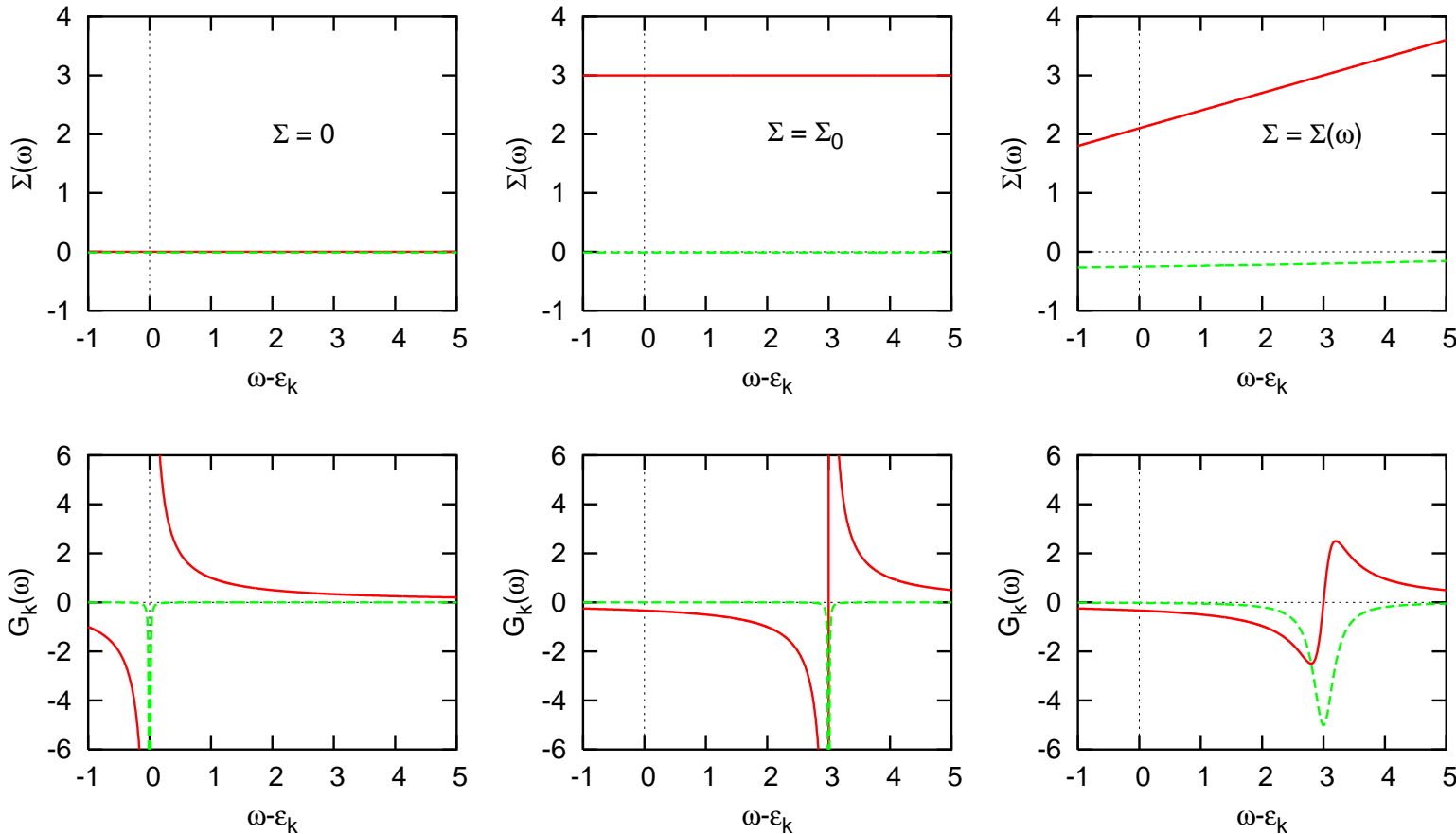


DMFT: $Z = \infty$

Excursus: Green function and self-energy

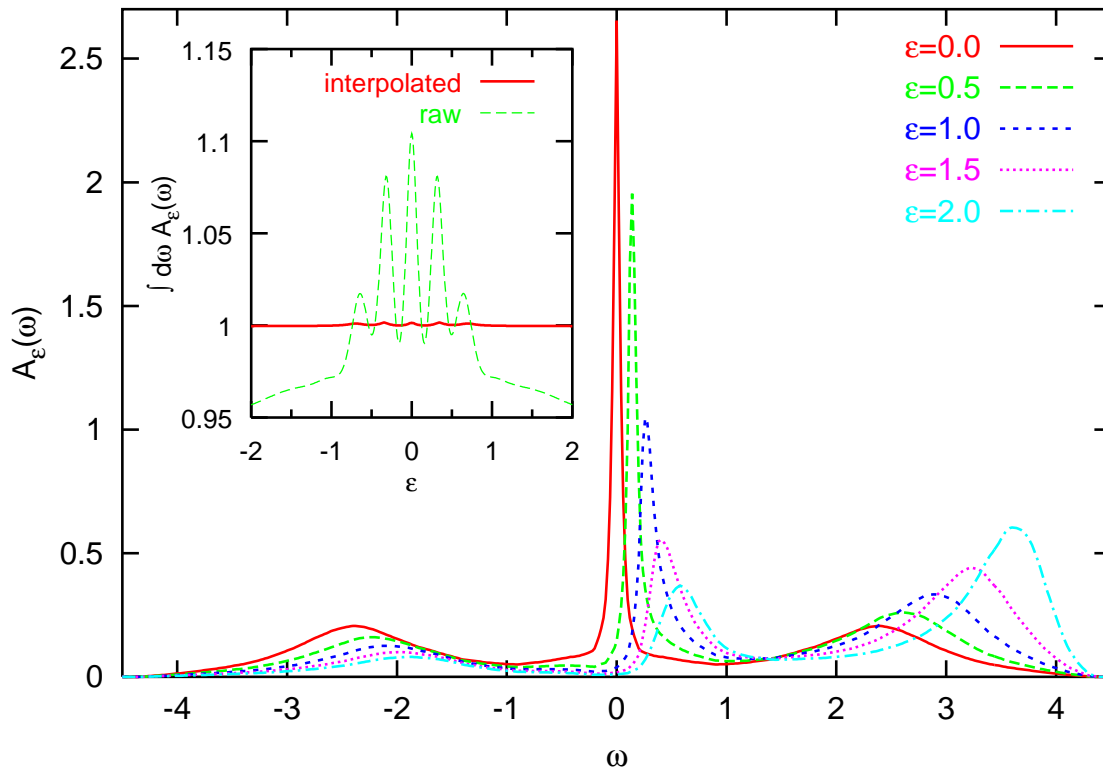
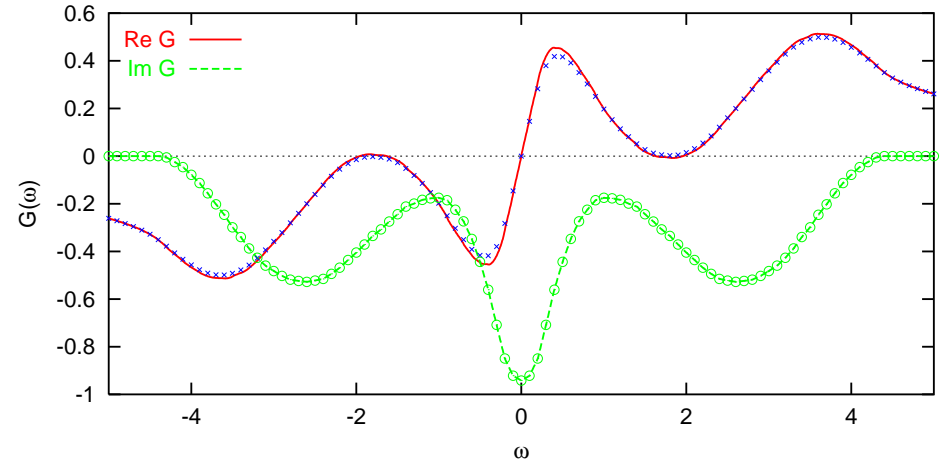
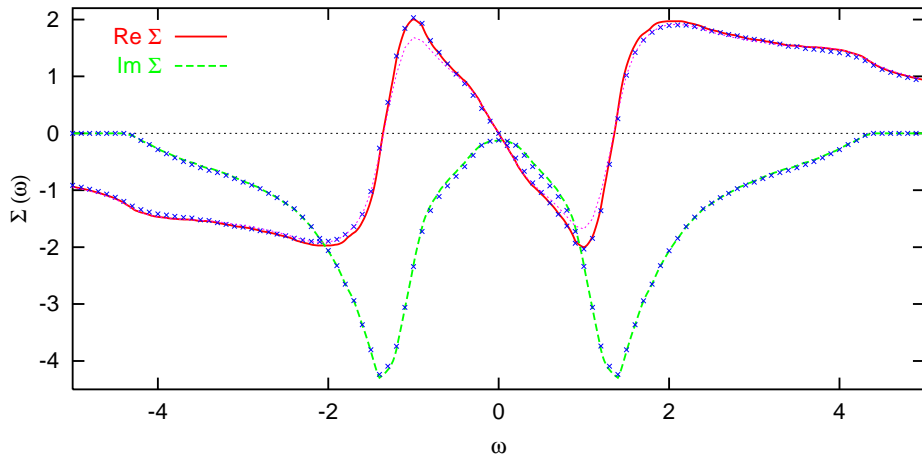
Noninteracting (1-band) system: dispersion $\epsilon_{\mathbf{k}}$, density of states $\rho(\epsilon) = \frac{1}{V_B} \int d^3k \delta(\epsilon - \epsilon_{\mathbf{k}})$

Green function (within DMFT for $\mu = 0$): $G_{\mathbf{k}}(\omega) = \frac{1}{\omega - \epsilon_{\mathbf{k}} - \Sigma(\omega)} = \frac{(\omega - \epsilon_{\mathbf{k}} - \Sigma') + i\Sigma''}{(\omega - \epsilon_{\mathbf{k}} - \Sigma')^2 + \Sigma''^2}$

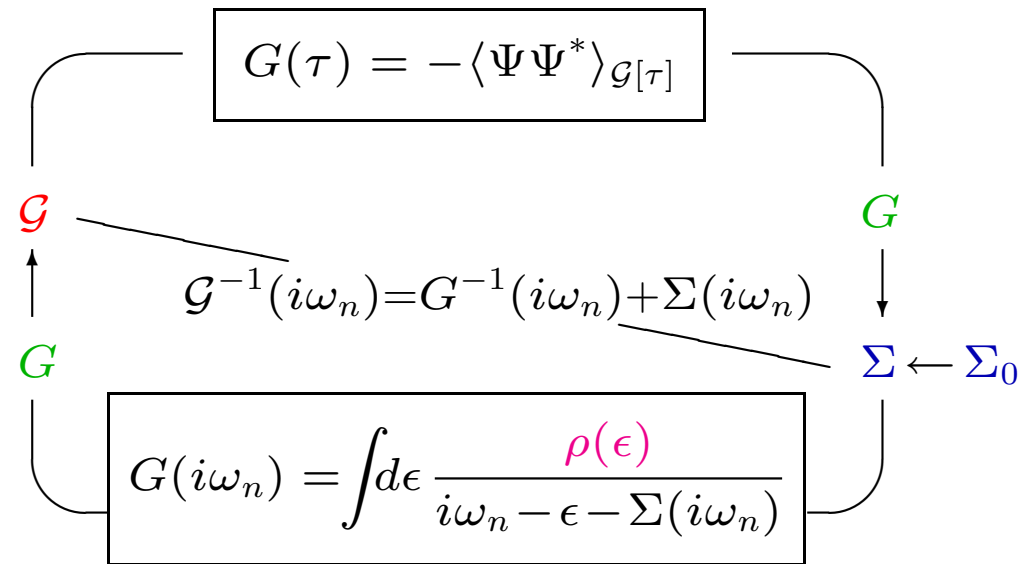


$$A(\omega) = -\frac{1}{\pi} \text{Im} G(\omega + i0^+) \xrightarrow{\Sigma \rightarrow 0} \rho(\omega); \quad G(\omega) \equiv G_{ii}(\omega) = \int d\epsilon \frac{\rho(\epsilon)}{\omega - \epsilon - \Sigma(\omega)}$$

Example: half-filled frustrated Hubbard model, $U=W=4$, $T=0.05$

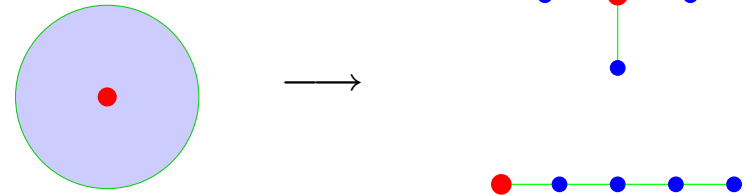


Iterative solution of DMFT equations



Impurity solver:

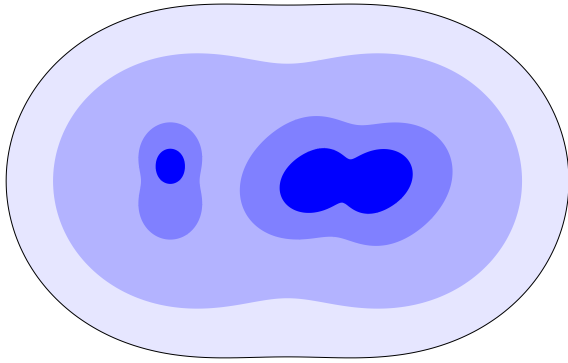
- Quanten-Monte-Carlo (QMC)
- Iterative perturbation theory (IPT; not controlled)
- Non-crossing approximation (NCA; not controlled)
- Exact diagonalization (ED; large finite-size errors)
- Numerical renormalization group (NRG; 1-2 bands)
- Density matrix renormalization group (DMRG)
- Self-energy functional theory (SFT) + ED



Direct $d = \infty$ solution: PT, ePT

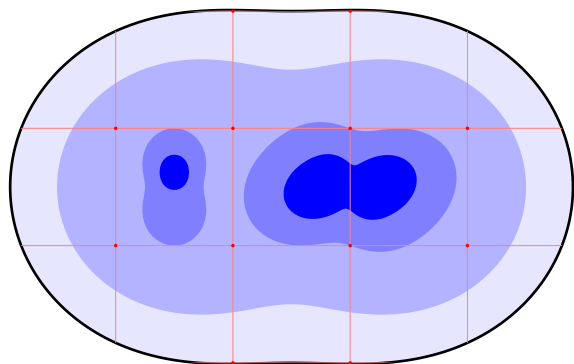
Excursus: Monte-Carlo Principles

Example: Computation of average depth \bar{h} of a lake from depth distribution $h(x_1, x_2)$



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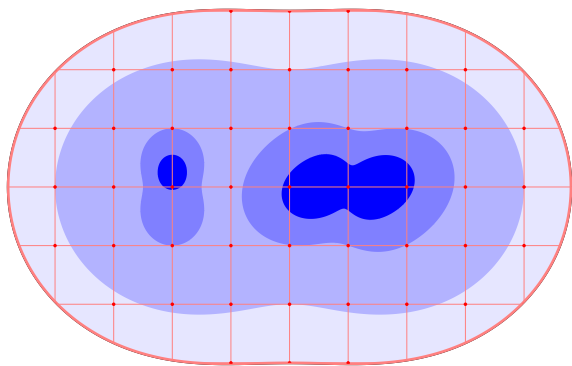
Deterministic: lattice + trapezoid rule

$N = V/(\Delta x)^d$ measurements

$$\Delta h \propto (\Delta x)^2 \propto N^{-2/d}$$

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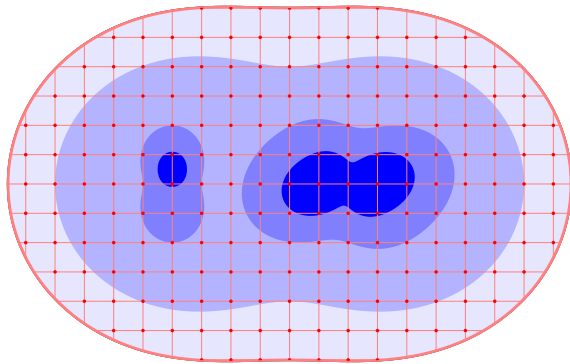
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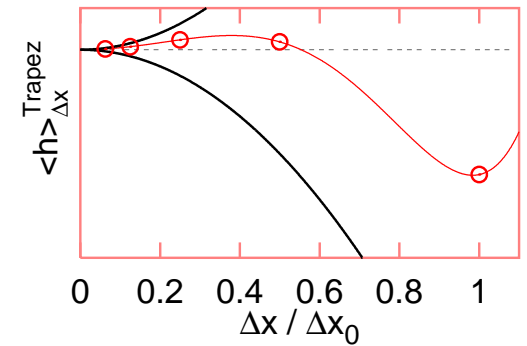
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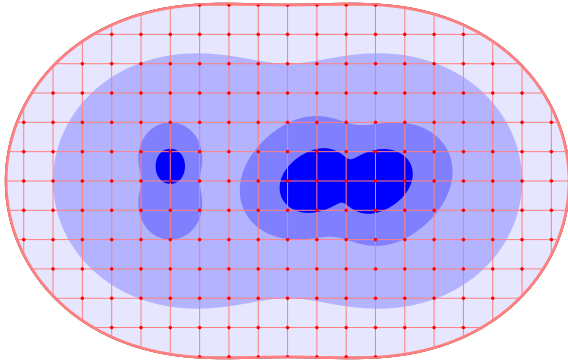
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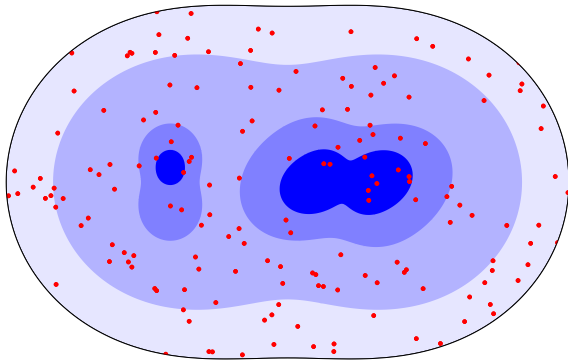
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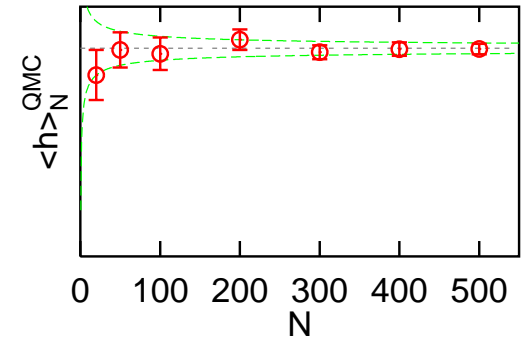
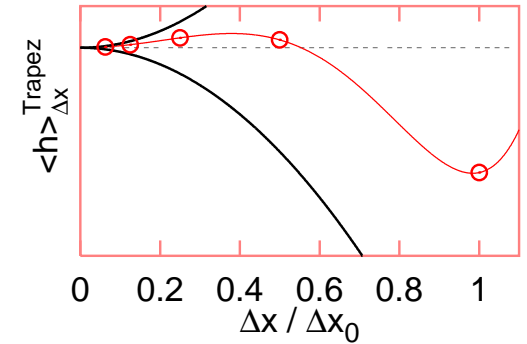
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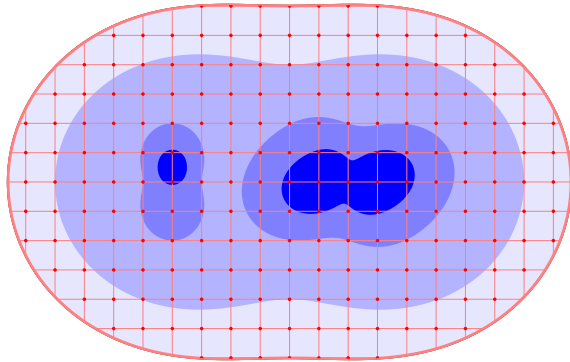
Stochastic: **simple Monte-Carlo**
 N "configurations", equally probable

$$\Delta h \lesssim \sqrt{\frac{\text{var}\{h\}}{N}} \propto N^{-1/2}$$



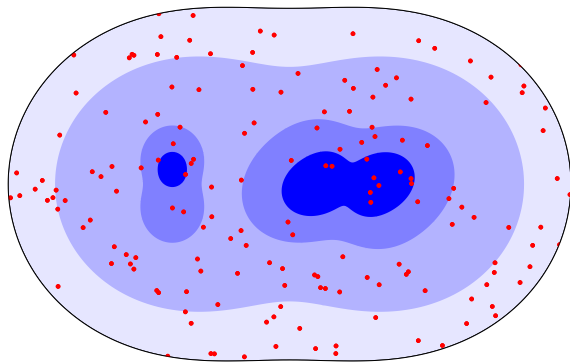
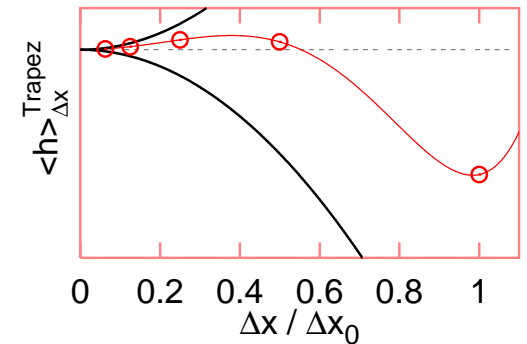
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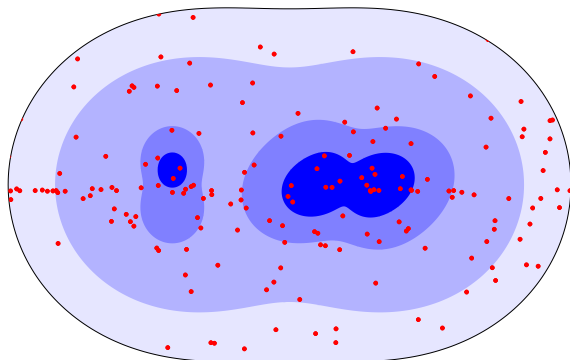
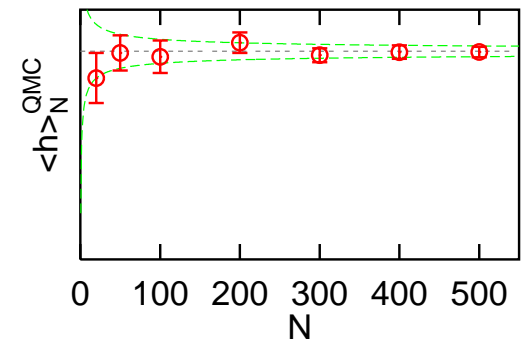
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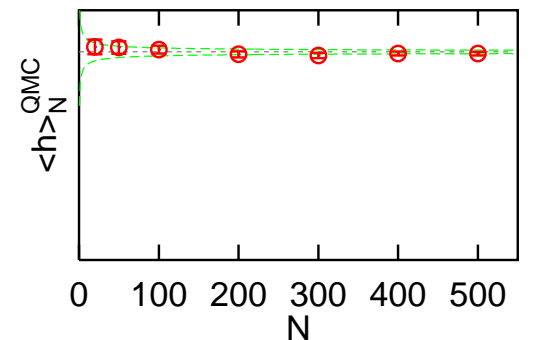
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Stochastic: **Importance sampling MC**
 factorization: $h(\mathbf{x}) = p(\mathbf{x}) o(\mathbf{x})$;
 $p(\mathbf{x})$ normalized, $\text{var}\{o\} \ll \text{var}\{h\}$

$$\Delta h \lesssim \sqrt{\frac{\text{var}\{o\}}{N_{\text{eff}}}} \propto N^{-1/2}$$



Application of Monte Carlo in Statistical Physics

$$\langle O \rangle = \sum_i p_i O_i, \quad p_i = \frac{e^{-E_i/(k_B T)}}{\mathcal{Z}} \equiv \frac{\tilde{p}_i}{\mathcal{Z}}, \quad \mathcal{Z} = \sum_i e^{-E_i/(k_B T)}$$

Simple Monte Carlo: Estimation of both sums from a number N of equally probable configurations.

Problem: typically $\sqrt{\text{var}\{p\}} \gg \bar{p}$.

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Importance Sampling MC: Probability distribution given by **Boltzmann weights** p_i .

Problem: Normalization $1/\mathcal{Z}$ unknown.

Solution: generate probability distribution by *random walk*, e.g. using **Metropolis algorithm**:

$$P\{i \rightarrow j\} = \min\{p_j/p_i, 1\}, \quad p_j/p_i = e^{(E_j - E_i)/(k_B T)}$$

$$\langle O \rangle = \frac{\sum_i \tilde{p}_i O_i}{\sum_i \tilde{p}_i} \longrightarrow \langle O \rangle = \sum_i O_i \approx \sum_{n=1+N_0}^{N+N_0} O_{in}; \quad \langle (\Delta O)^2 \rangle \propto \frac{\text{var}\{O\}}{N}$$

+ Precise computation of observable averages $\langle O \rangle$

– Not accessible by construction: partition function \mathcal{Z} , free energy F

Hirsch-Fye QMC algorithm for DMFT impurity problem

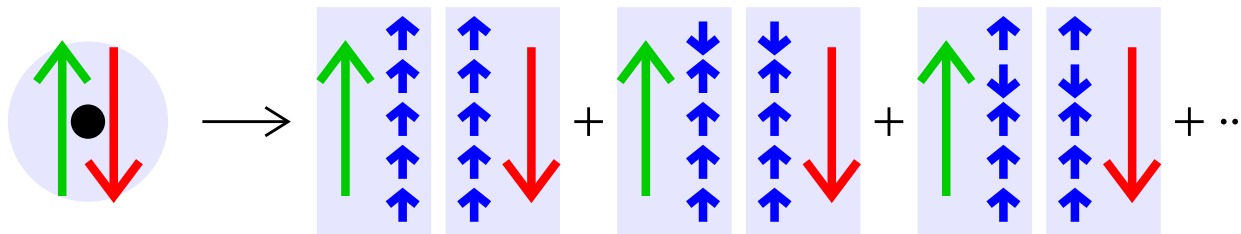
Wanted: Green-Funktion $G(\omega)$

Treatment in **imaginary time** using fermionic Grassmann variables ψ, ψ^* :

$$G_\sigma(\tau_2 - \tau_1) \equiv G_\sigma(\tau_1, \tau_2) = \frac{1}{\mathcal{Z}} \int \mathcal{D}[\psi] \mathcal{D}[\psi^*] \psi_\sigma(\tau_1) \psi_\sigma^*(\tau_2) e^{\mathcal{A}},$$

$$\mathcal{A} = \mathcal{A}_0 - \frac{U}{2} \sum_{\sigma\sigma'} \int_0^\beta d\tau \psi_\sigma^*(\tau) \psi_\sigma(\tau) \psi_{\sigma'}^*(\tau) \psi_{\sigma'}(\tau)$$

discretization $\beta = \Lambda \Delta\tau$, Trotter decoupling, discrete Hubbard-Stratonovich transformation



Wick theorem:

$$G = \frac{\sum M \det\{M\}}{\sum \det\{M\}}$$

Metropolis MC importance sampling over **auxiliary Ising field**, 2^Λ configurations, $50 \lesssim \Lambda \lesssim 400$

+ nonperturbative, numerically exact

– effort scales as T^{-3}

Hirsch-Fye QMC algorithm for DMFT impurity problem

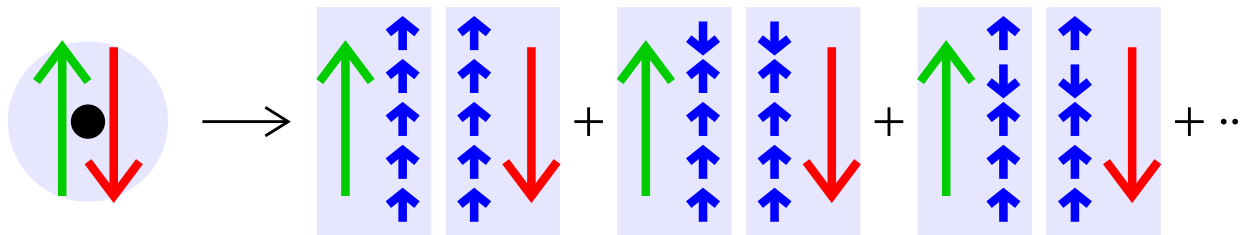
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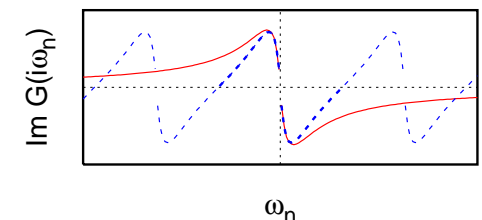
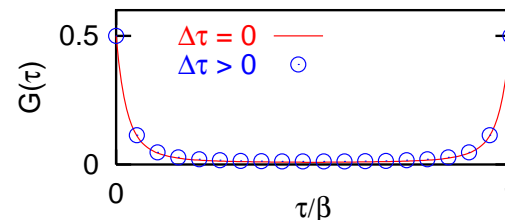


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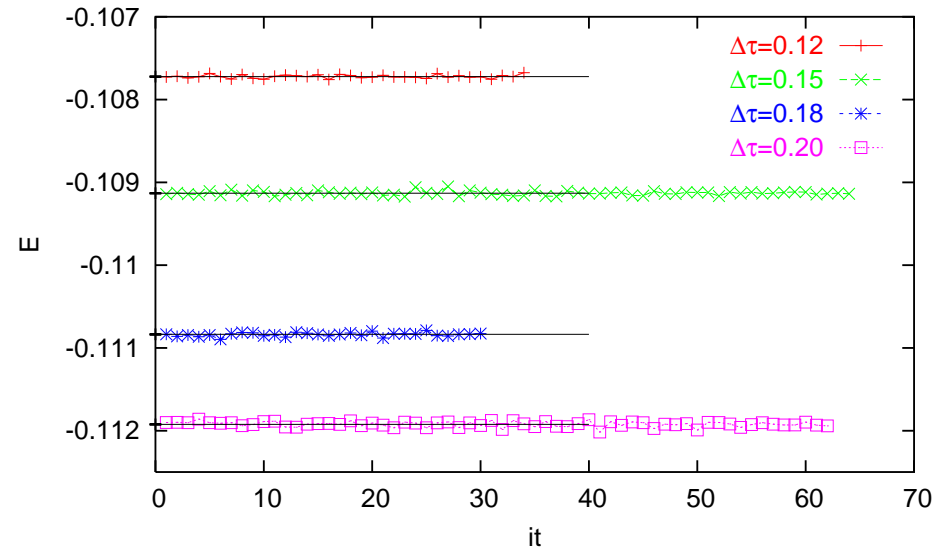
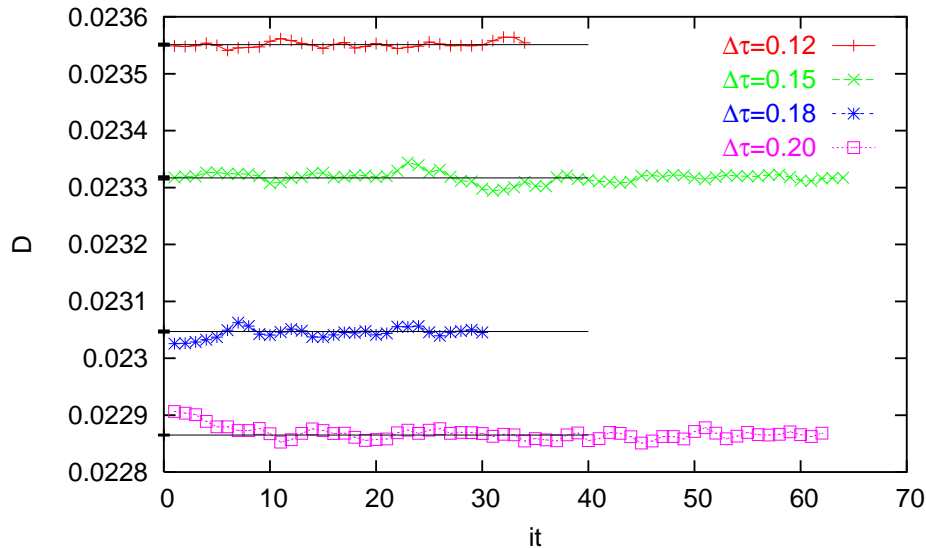
- + nonperturbative, numerically exact
- effort scales as T^{-3}
- no information for $\omega \gtrsim \omega_{\text{Nyquist}}$



Contributions to DMFT-QMC error bars:

- statistical fluctuations + warm-up
- convergency (of self-consistency cycle)
- discretization (Trotter error and Fourier transform)

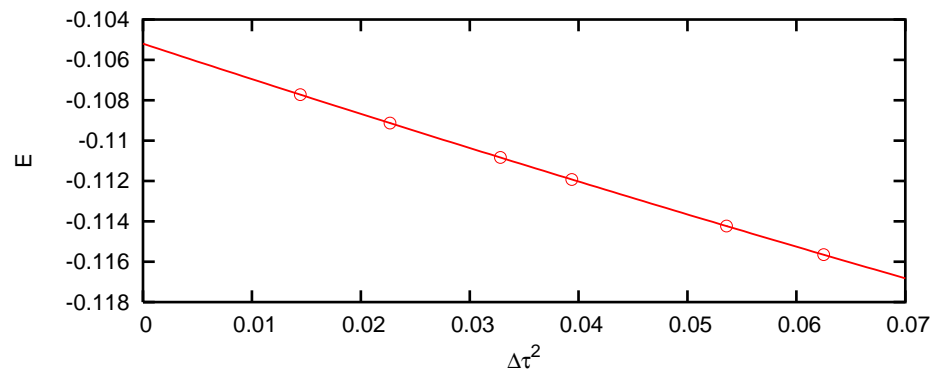
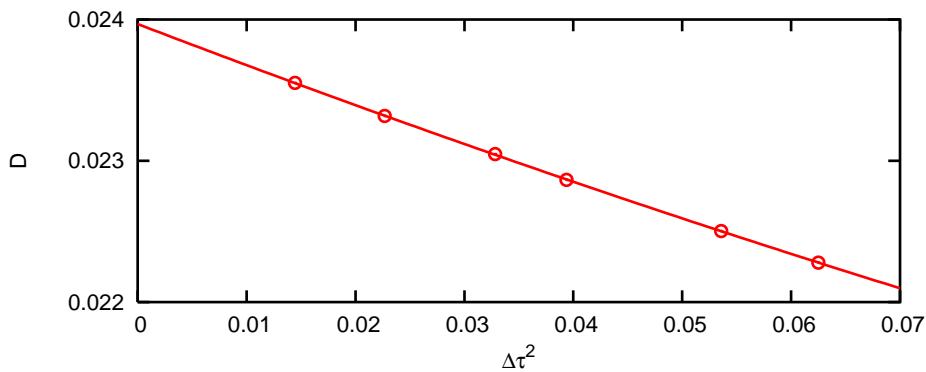
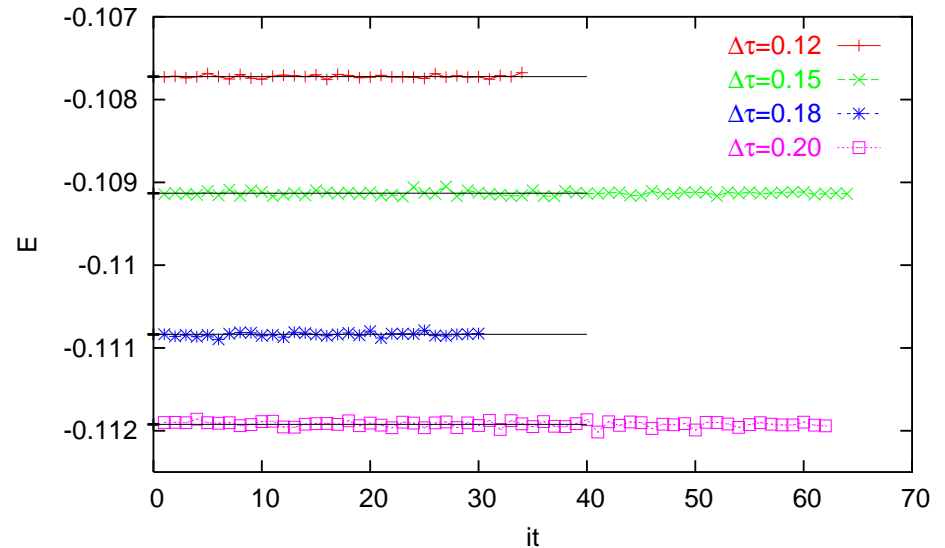
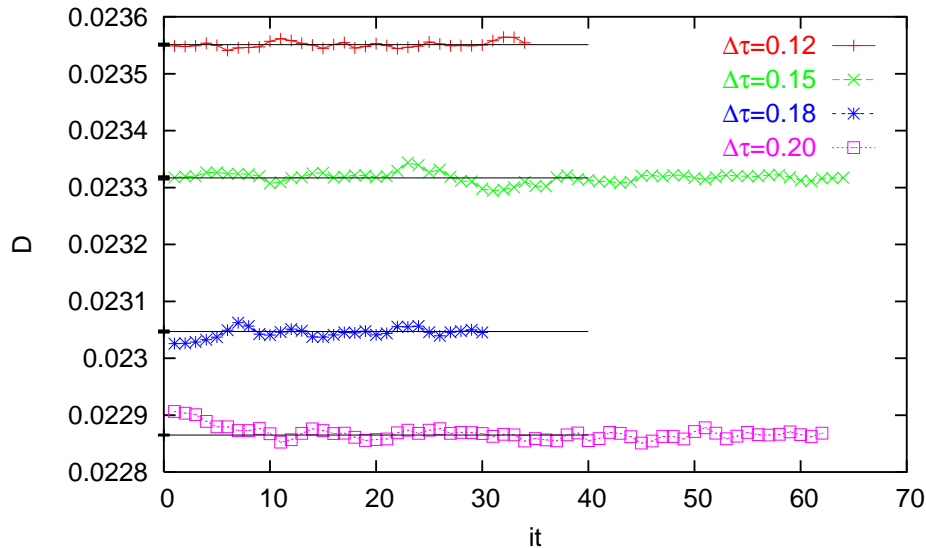
Example: half-filled frustrated Hubbard model, $U = 5$, $W = 4$, $T = 0.04$ (Mott insulator)



Contributions to DMFT-QMC error bars:

- statistical fluctuations + warm-up
- convergency (of self-consistency cycle)
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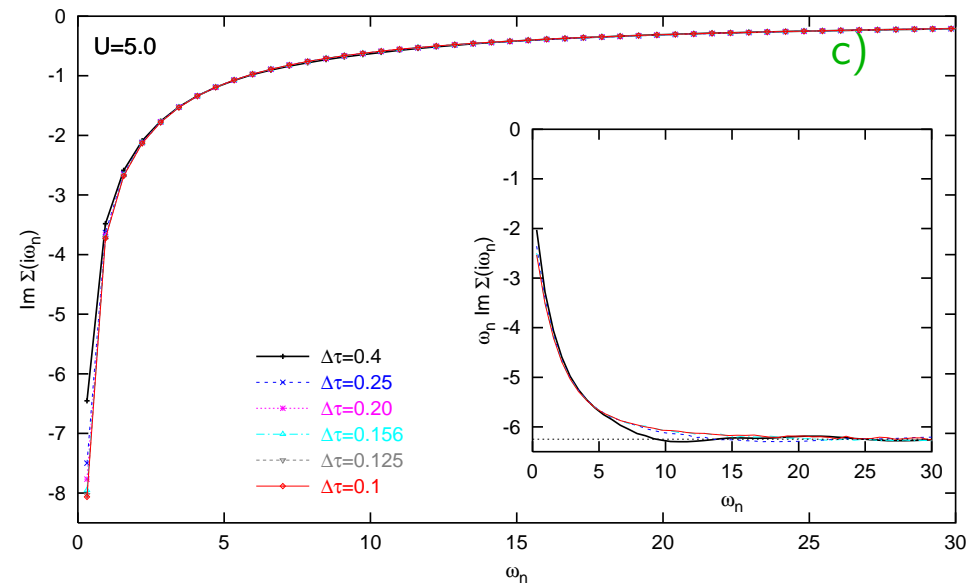
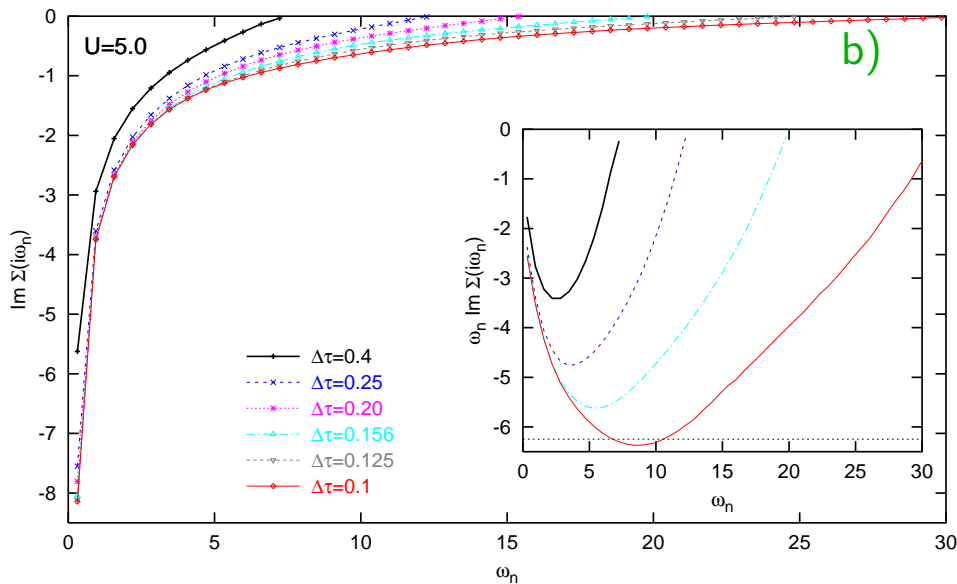
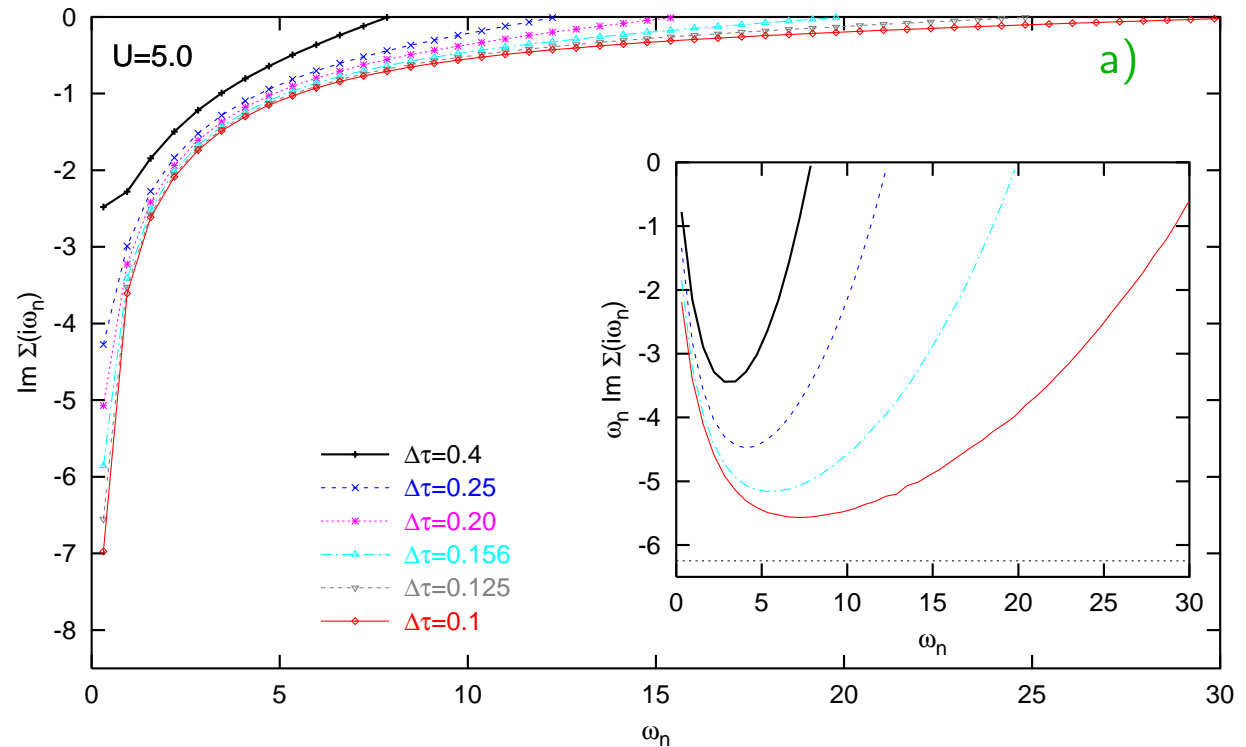
next: prerequisite for / proof of extreme precision

Fourier transformation schemes:
 self-energy ($T = 0.1, U = 5.0$)

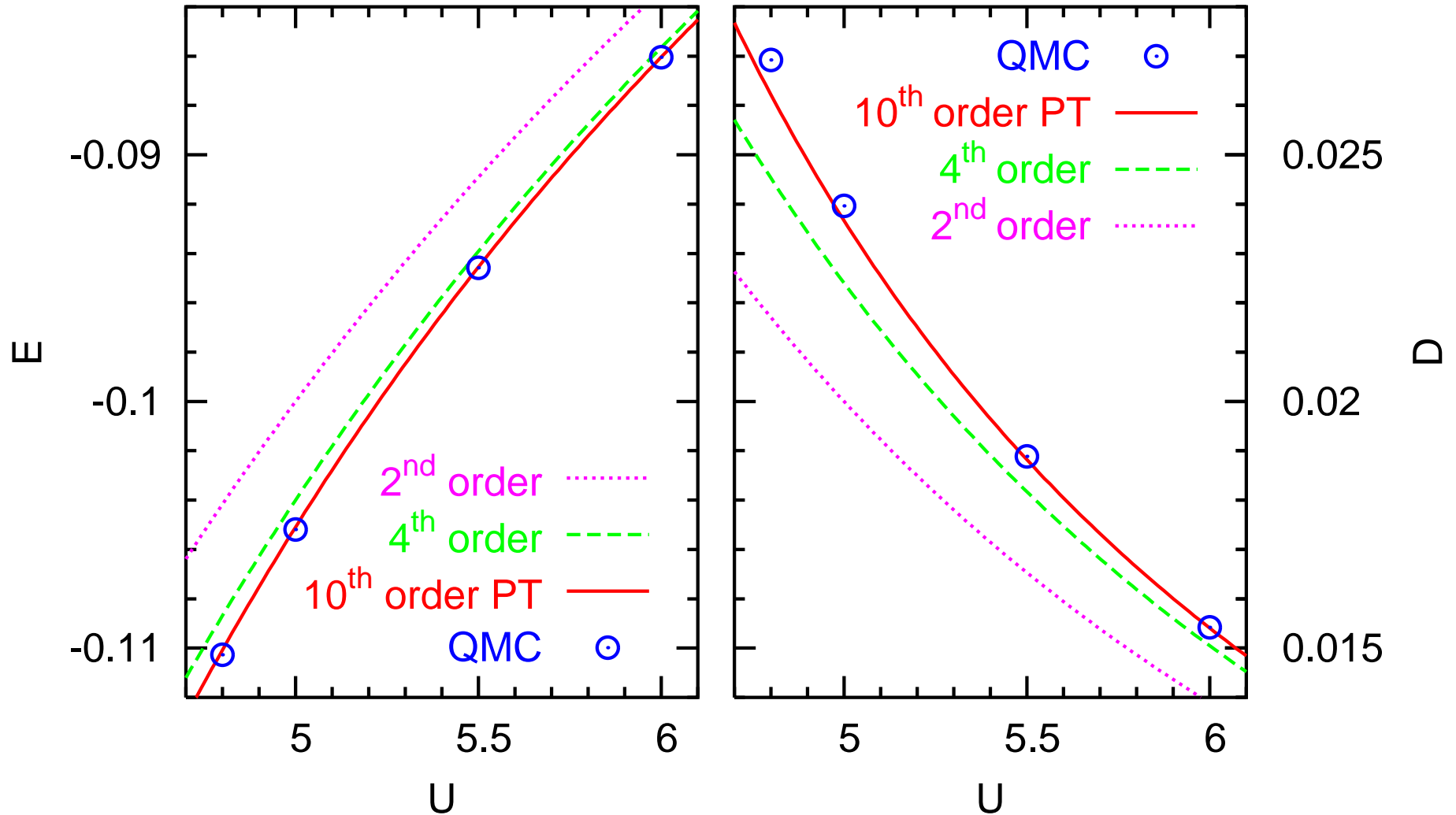
- a) "Ulmke smoothing",
- b) improved "Smoothing",
- c) scheme with analytic high-frequency corrections

even stronger effects at lower T

low-frequency errors of $\Sigma(\omega)$ small
 in b) und c)

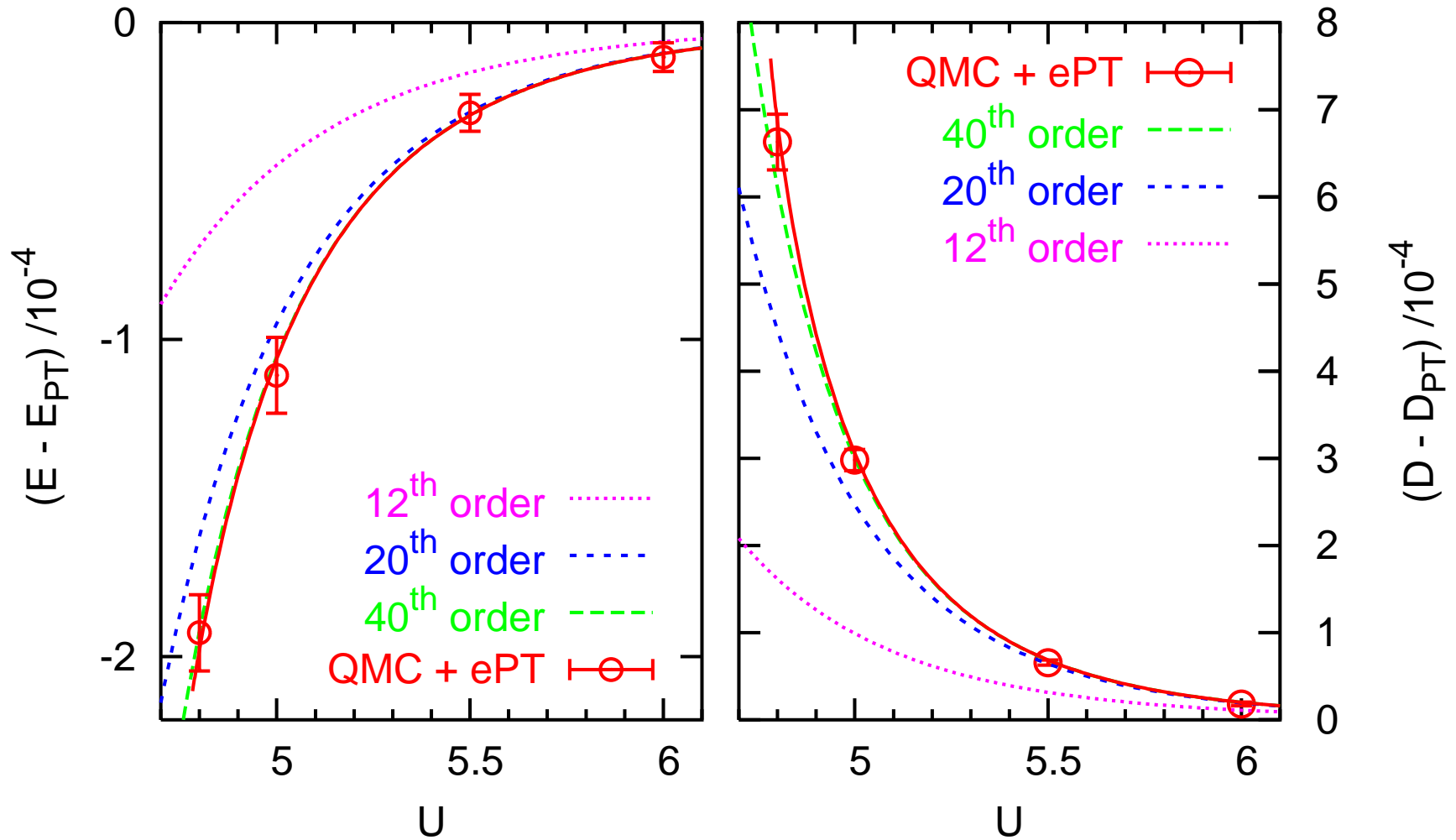


Mott insulator: energy + double occupancy I



Excellent agreement at $U = 6.0$.

Mott insulator: energy + double occupancy II



Mott insulator: U_{c1} , critical exponents, low- T parameter for $U_c(T)$

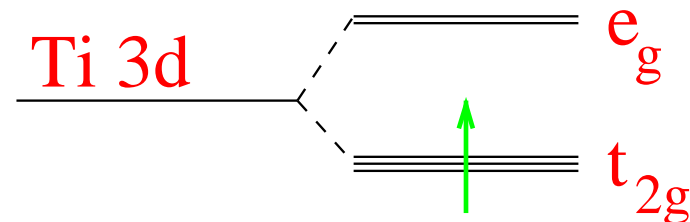
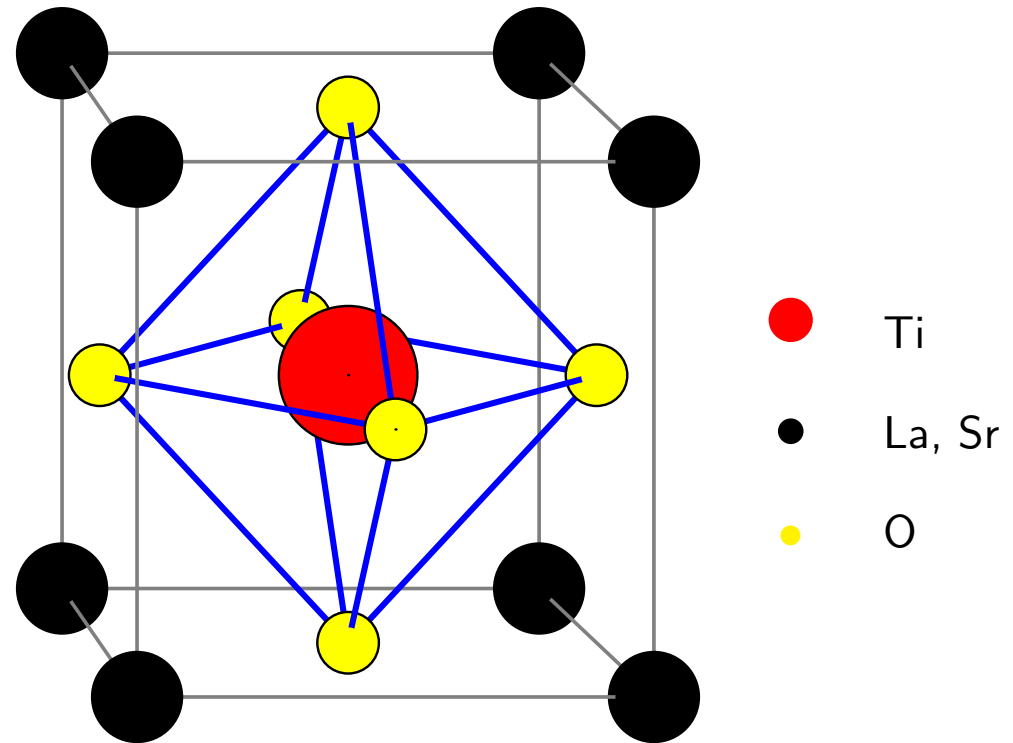
high-precision results for E , D at all U (parametrizations available) \rightsquigarrow benchmark

[Blümer, Kalinowski, cond-mat/0404568 (2004), cond-mat/0407442 (2004)]

Realistic LDA+DMFT(QMC) calculations

$\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$

- perovskite structure
- $1-x$ t_{2g} electrons per site
- AF for $x \lesssim 0.05$
- strongly correlated metal
- density functional theory (LDA) fails



multi-band issues

$\frac{2M(2M-1)}{2}$ Hubbard-Stratonovich fields

approximation: Hund terms $J_{\alpha\alpha'} \mathbf{s}^\alpha \cdot \mathbf{s}^{\alpha'} \longrightarrow J_{\alpha\alpha'} s_z^\alpha s_z^{\alpha'}$ to avoid sign problem in QMC

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Analytic continuation

Aim: (ill-conditioned) inversion of $G(\tau) = \int d\omega \frac{\exp[-\tau\omega]}{1 + \exp[-\beta\omega]} A(\omega)$

Maximum entropy method (MEM): introduce entropy function to find smoothest solution $A(\omega)$ compatible with $G(\tau)$

$$G(\tau) \xrightarrow{\text{MEM}} \text{Im}G(\omega) \xrightarrow{\text{Kra-Kro}} \text{Re}G(\omega)$$

MEM: not fully controlled; no $\Delta\tau$ extrapolation possible

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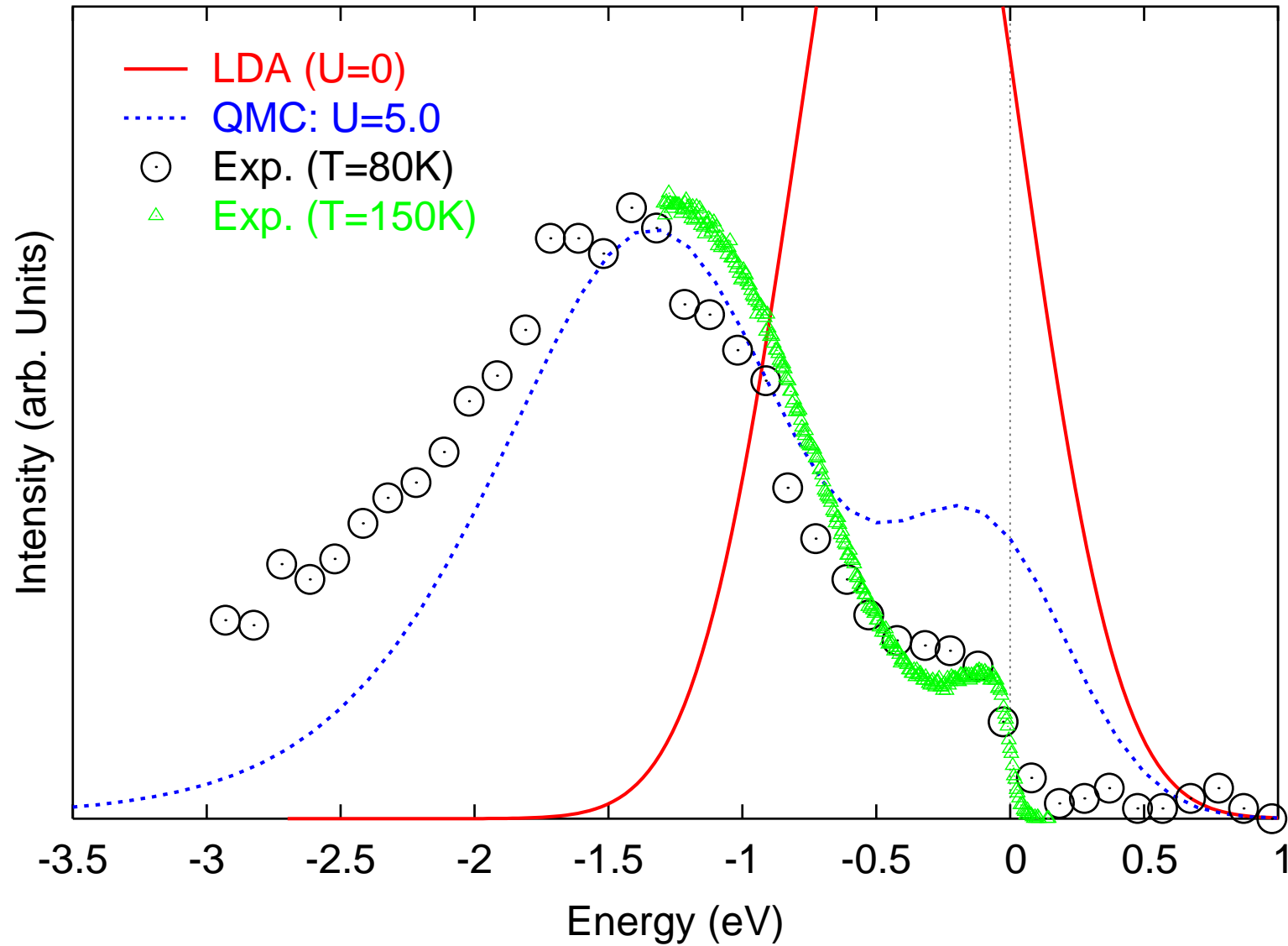
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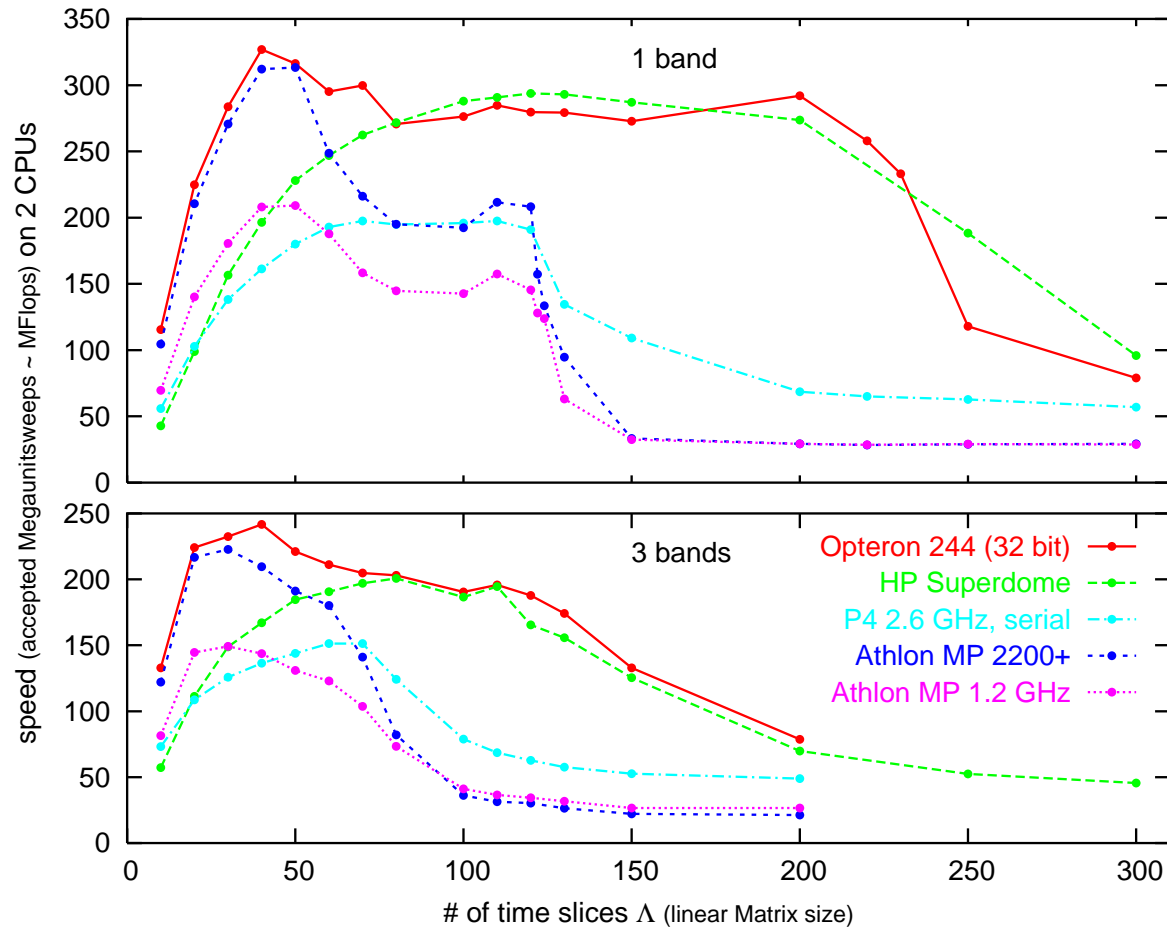
for ARPES, $\sigma(\omega)$: use 2-dimensional Newton scheme to invert Dyson equation for $G(\omega) \longrightarrow \Sigma(\omega)$

Photoemission spectra for $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$ ($x=0.06$)



[Nekrasov, Held, Blümer, Poteryaev, Anisimov, Vollhardt, EPJB **18**, 55 (2000)]

Computers



Group cluster (2nd stage)



JUMP cluster (NIC Jülich)

Summary

“derivation” of (1-band/multi-band) Hubbard model

characterization of DMFT

role of self-energy

Monte Carlo principles

QMC: principles and caveats (convergency, $\Delta\tau$ extrapolation)

extreme-precision QMC results for 1-band model (vs. ePT, SFT/DIA)

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LDA+DMFT: significant improvements for PES of $\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$

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DMFT for double perovskite models

Further talks: high-frequency corrected QMC (multi-band); observables
MEM and LDA+DMFT